In The Amazing Spider-Man, his Spidey sense—and his adoption story—are tingling